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Laws of logarithms

$$\log_b(M \cdot N) = \log_b(M) + \log_b(N)$$

$$\log_b\left(\frac{M}{N}\right) = \log_b(M) - \log_b(N)$$

$$\log_b(M^k) = k \cdot \log_b M$$

Express in terms of $\log_b M$ and $\log_b(N)$

Ex ① $\log_b(M^2 N^3)$

$$= \log_b(M^2) + \log_b(N^3)$$
$$= 2\log_b(M) + 3\log_b(N)$$

② $\log_b\left(\sqrt{\frac{M}{N^5}}\right)$

$$= \log_b\left(\frac{M^{1/2}}{N^{5/2}}\right)$$

$$= \log_b(M^{1/2}) - \log_b(N^{5/2})$$

$$= \frac{1}{2}\log_b(M) - \log_b(N^{5/2})$$

If $\log_{10}(9) = .95$ and $\log_{10}(2) = .30$ find the following

Ex ③

$$\log_{10}(3)$$

$$\log_{10}(9^{1/2})$$

$$\frac{1}{2}\log_{10}(9)$$

$$\frac{1}{2}(.95) = \boxed{.475}$$

④

$$\log_{10}(900)$$

$$\log_{10}(9 \cdot 100)$$

$$\log_{10}(9) + \log_{10}(100)$$

$$.95 + 2$$

$$\boxed{2.95}$$

$$\log_{10}(100) = x$$

$$10^x = 100$$

$$10^x = 10^2$$

$$x = 2$$